

## FINDING GCFs and LCMs Using the Venn Diagram

Example 1: Find the GCF and LCM for 50 and 60.

- 1) Use any method to factor each number. (Examples: Factor trees, or stair steps or ...).
- 2) Then, write the prime factorization for each number.

$$\text{Factor 50: } 2 \times 5 \times 5$$

$$\text{Factor 60: } 2 \times 3 \times 2 \times 5 = 2 \times 2 \times 3 \times 5$$

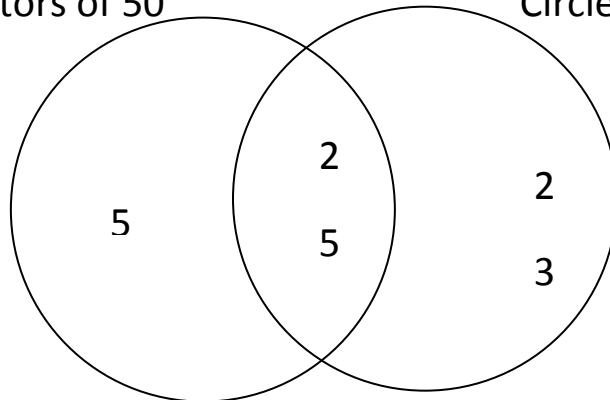
- 3) Start with the factors of 50.  
The first factor is 2.  
Since 2 also is a factor of 60, you put that in the “football shape”, the intersection of the two circles.
- 4) Then, cross it off each expanded problem. (2 is a common factor.)
- 5) Do the same thing for the rest of the factors until they have no other factors in common. (5 is also a common factor.)
- 6) The factors that are “left over” belong in the part of the circle that is not overlapping.
- 7) Circle A has all the factors of 50. Circle B has all the factors of 60. The overlapping part contains the factors that are in common with both numbers.

$$\text{Factor 50: } \cancel{2} \times \cancel{5} \times 5$$

$$\text{Factor 60: } \cancel{2} \times 3 \times 2 \times \cancel{5} = 2 \times 2 \times 3 \times 5$$

Circle A: Factors of 50

Circle B: Factors of 60



$$\text{GCF for 50 and 60} = 2 \times 5 = 10$$

Then for LCM, multiply all the numbers together that are in the Venn Diagram:

$$\text{LCM for 50 and 60: } 5 \times 2 \times 5 \times 2 \times 3 = 300$$

Example 2: Find the GCF and LCM of 24 and 36:

Use trees or any method to factor each number. Write the prime factorization.

$$\text{Factor 24: } 2 \times 2 \times 2 \times 3$$

$$\text{Factor 36: } 2 \times 2 \times 3 \times 3$$

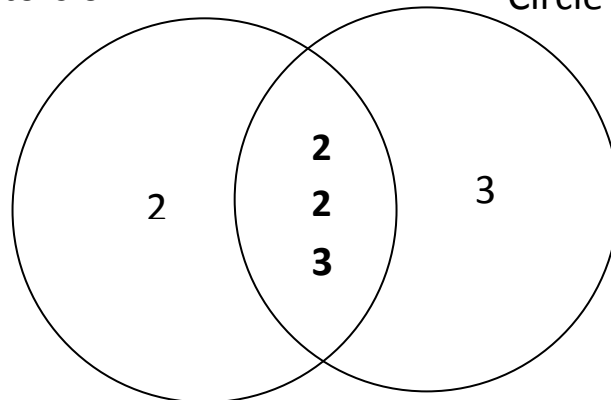
Cross out the common factors and put them in the "intersection" of the Venn Diagram

$$\text{Factor 24: } \cancel{2} \times \cancel{2} \times 2 \times \cancel{3}$$

$$\text{Factor 36: } \cancel{2} \times \cancel{2} \times \cancel{3} \times 3$$

Circle A: Factors of 24

Circle B: Factors of 36



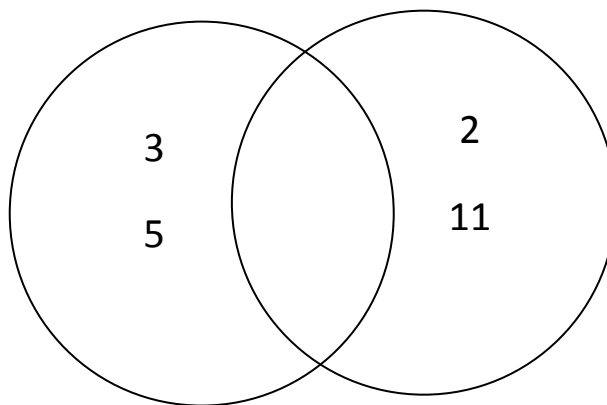
$$\text{GCF: } 2 \times 2 \times 3 = 12$$

$$\text{LCM: } 2 \times 2 \times 2 \times 3 \times 3 = 72$$

Example 3: Find the GCF and LCM of 15 and 22.

$$\text{Factor 15: } 3 \times 5$$

$$\text{Factor 22: } 2 \times 11$$



What is a factor of every number? 1!!! Since these two numbers don't have any other factors in common, the GCF is 1.

$$\text{LCM: } 3 \times 5 \times 2 \times 11 = 330$$